Geometry

Big Ideas Chapter 3 Study Guide - Parallel and Perpendicular Lines

Definitions

Parallel lines (||): lines are coplanar and do not intersect. **Perpendicular lines** (\perp): lines that intersect at 90° angles. **Skew lines**: lines that are not coplanar. They are not parallel and they do not intersect.

Parallel planes: planes that do not intersect. **Transversal**: a line that intersects two coplanar lines at two different points.

Corresponding angles: like $\angle 1$ and $\angle 5$

Exterior Interior Exterio

Alternate interior angles: like $\angle 4$ and $\angle 5$ Alternate exterior angles: like $\angle 1$ and $\angle 8$ Consecutive (Same-side) interior

Consecutive (Same-side) interior angles: like $\angle 3$ and $\angle 5$ **Perpendicular bisector**: a line perpendicular to a segment at the segment's midpoint.

Theorems and Postulates

Parallel Postulate: If there is a line and a point not on the line, then there is exactly one line through the point parallel to the given line.

Perpendicular Postulate: If there is a line and a point not on the line, then there is exactly one line through the point perpendicular to the given line.

Corresponding Angles Theorem: If two parallel lines are cut by a transversal, then the pairs of corresponding angles are congruent. The converse is also true.

Alternate Interior Angles Theorem: If two parallel lines are cut by a transversal, then the pairs of alternate interior angles are congruent. The converse is also true.

Alternate Exterior Angles Theorem: If two parallel lines are cut by a transversal, then the two pairs of alternate exterior angles are congruent. The converse is also true.

Same-side (Consecutive) Interior Angles Theorem: If two parallel lines are cut by a transversal, then the two pairs of same-side interior angles are supplementary. The converse is also true.

Linear Pair Perpendicular Theorem: If two lines intersect to form a linear pair of congruent angles, then the lines are perpendicular. **Perpendicular Transversal Theorem**: In a plane, if a transversal is perpendicular to one of two parallel lines, then it is perpendicular to the other line.

Lines Perpendicular to a Transversal Theorem: In a plane, if two lines are perpendicular to the same line, then they are parallel to each other.

Slopes of Parallel Lines Theorem: In a coordinate plane, two distinct non-vertical lines are parallel if and only if they have the same slope.

Slopes of Perpendicular Lines Theorem: In a coordinate plane, two non-vertical lines are perpendicular if and only if the product of their slopes is -1.

Distance from a point to a line: the length of the perpendicular segment from the point to the line (A to B).



Constructions

Parallel lines (P. 139)





Perpendicular bisector (P. 149)



Geometry Big Ideas Chapter 3 Practice Problems Show all work!!!

1) If the figure shown is folded to form a cube, which faces of the cube will be parallel?







Reasons

3) Given: $m \angle 2 + m \angle 3 = 180^\circ$. Prove: $\ell \mid \mid m$.





Statements

4) In the figure, find x and y.



6) A right triangle is formed by the x-axis, the y-axis, and the line $y = -\frac{3}{4}x + 15$. Find the length of the hypotenuse.

5) $\overrightarrow{ST} \parallel \overrightarrow{VW}$ for S(-3, 5), T(1, -1), V(x, -3), and W(1, y). Find values for x and y.

7) Are the points (-2, -4), (5, -2), and (2, -3) collinear? Explain the method you used to determine the answer.

8) Find the point-slope form of the perpendicular bisector of the segment with endpoints (-6, 3) and (4, -5).

9) Construct a perpendicular to segment \overline{AB} through point X.

